

Lesson 43 MR12

Aim: How do we apply the exponential function?

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Do Now:

John bought an antique for \$1000. The value of the antique has a 10% fixed increasing rate annually. Find the value of the antique after

a) 1 year b) 2 years c) 5 years d) 10 years

Answers:

$$A = 1000(1 + 0.1)^5$$

$$= 1000(1.61051) = 1610.51$$

$$A = 1000(1 + 0.1)^{10} = 1000(1.1)^{10}$$

$$= 1000(2.5937) = 2593.7$$

Jan 5-9:07 AM

Exponential Growth:

$$A = A_0(1 + r)^t$$

A is the amount after certain number of years

A_0 is the initial amount

r is the rate

t is the number of years

Jan 5-9:10 AM

Enrique won \$10,000 and decided to use it as a "vacation fund." each summer, he withdraws an amount of money that reduces the value of the fund by 7.5% from the previous summer. How much will the fund be worth after the tenth withdrawal?

This problem is **decay** situation

Use the formula $A = A_0(1 + r)^t$
with $A_0 = 10,000$, $r = -0.075$ and $t = 10$.

$$A = 10,000(1 - 0.075)^{10} = 10,000(0.925)^{10}$$

$$= \mathbf{4,585.82}$$

Jan 5-9:15 AM

To find the **compound interest**, we use n is number of times compounded per year. t is the number of years.

$$A = A_0 \left(1 + \frac{r}{n}\right)^{nt}$$

Marissa has \$2500 to deposit into a bank account. The interest rate is 4%. What is the difference if the money is compounded annually, monthly, or quarterly for 6 years?

Compounded

Annually

$$2500(1 + .04)^6$$

$$2500(1.04)^6$$

$$2500(1.2653)$$

$$3163.25$$

Monthly

$$2500\left(1 + \frac{.04}{12}\right)^{6(12)}$$

$$2500(1 + .0033)^{72}$$

$$2500(1.0033)^{72}$$

$$2500(1.2677)$$

$$3169.25$$

Quarterly

$$2500\left(1 + \frac{.04}{4}\right)^{6(4)}$$

$$2500(1 + .01)^{24}$$

$$2500(1.01)^{24}$$

$$2500(1.2697)$$

$$3174.25$$

Continuously

$$A = Pe^{rt} \text{ or } A = A_0e^{rt}$$

$$e = 2.71$$

$$2500e^{.04(6)}$$

$$2500e^{.24}$$

$$2500(1.2712)$$

$$3178$$

Jan 5-9:19 AM

In a state park, the deer population was estimated to be 2000 and increasing continuously at a rate of 4% per year. If the increase continues at that rate, what is the expected deer population in 10 years?

Since change takes place continuously

Use the formula $A = A_0 e^{rt}$.

Let $A_0 = 2000$,

$r = 0.04$, and $t = 10$.

$$A = 2000e^{(0.04)(10)} = 2000e^{0.4}$$

$$A = 2984$$

Jan 5-9:24 AM

The decay constant of radium is -0.0004 per year. How many grams will remain of a 50-gram sample of radium after 20 years?

Change is taking place continuously.

Use the formula $A = A_0 e^{rt}$.

$A_0 =$

$r =$

$t =$

$e =$

Jan 5-9:30 AM

Jan 5-1:44 PM